



НАЦИОНАЛЬНЫЙ ИССЛЕДОВАТЕЛЬСКИЙ ЦЕНТР «КУРЧАТОВСКИЙ ИНСТИТУТ»

**ПЕТЕРБУРГСКИЙ ИНСТИТУТ ЯДЕРНОЙ ФИЗИКИ им. Б.П.
Константинова**

From spiral to ferromagnetic structure in B20 compounds: role of cubic anisotropy

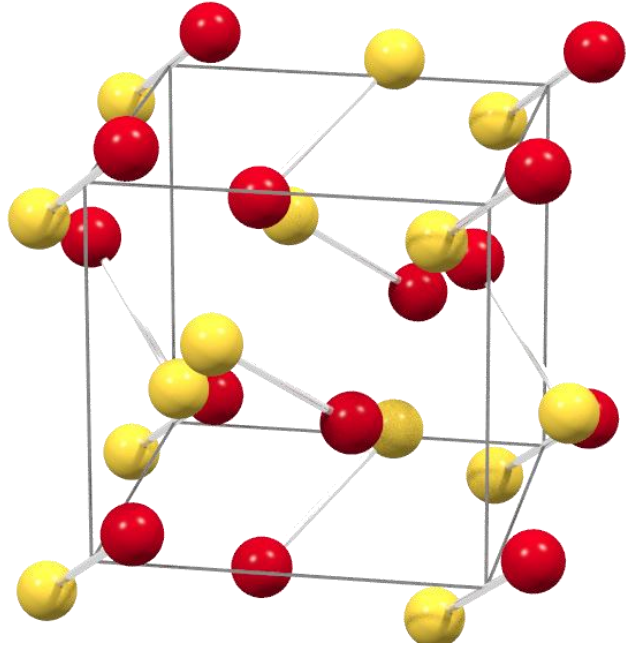
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B20 structure



Examples

MnSi, FeSi, CoSi

$\text{Mn}_{1-y}\text{Fe}_y\text{Si}$, $\text{Mn}_{1-y}\text{Co}_y\text{Si}$, $\text{Fe}_{1-x}\text{Co}_x\text{Si}$

MnGe, FeGe, CoGe

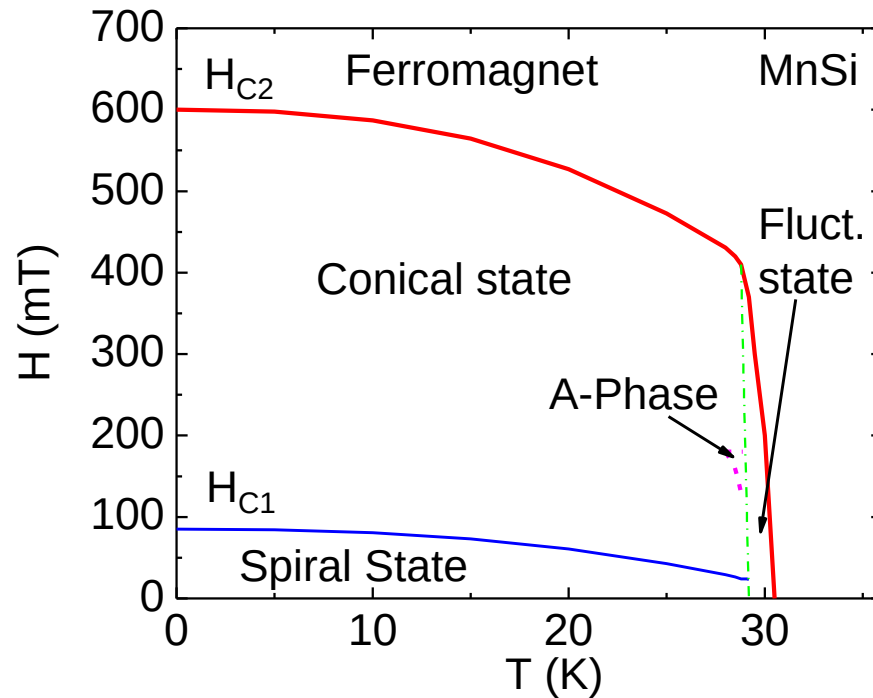
$\text{Mn}_{1-y}\text{Fe}_y\text{Ge}$, $\text{Fe}_{1-y}\text{Co}_y\text{Ge}$, $\text{Mn}_{1-y}\text{Co}_y\text{Ge}$



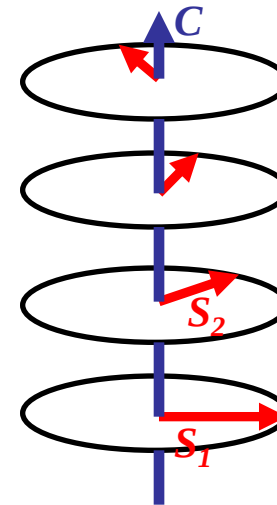
- B20-type cubic
- Space group $P2_13$, $a \approx 4.6 - 4.8 \text{ \AA}$
- 4 Me and 4 Si atoms are inside a unit cell
positions (u,u,u) , $(1/2+u,1/2-u,u)$, $(1/2-u,-u,1/2+u)$, $(-u,1/2+u,1/2+u)$ with $u_{\text{Mn}} = 0.138$ and $u_{\text{Si}} = 0.845$

B-T phase diagram in B20 compounds

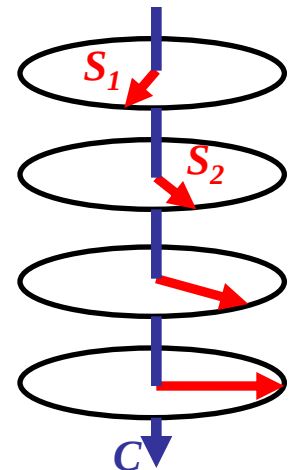
[1] Y. Ishikawa, G. Shirane, J.A. Tarvin, M. Kohgi,
Phys.Rev.B 16 (1977) 4956.



**Right-handed
helix**



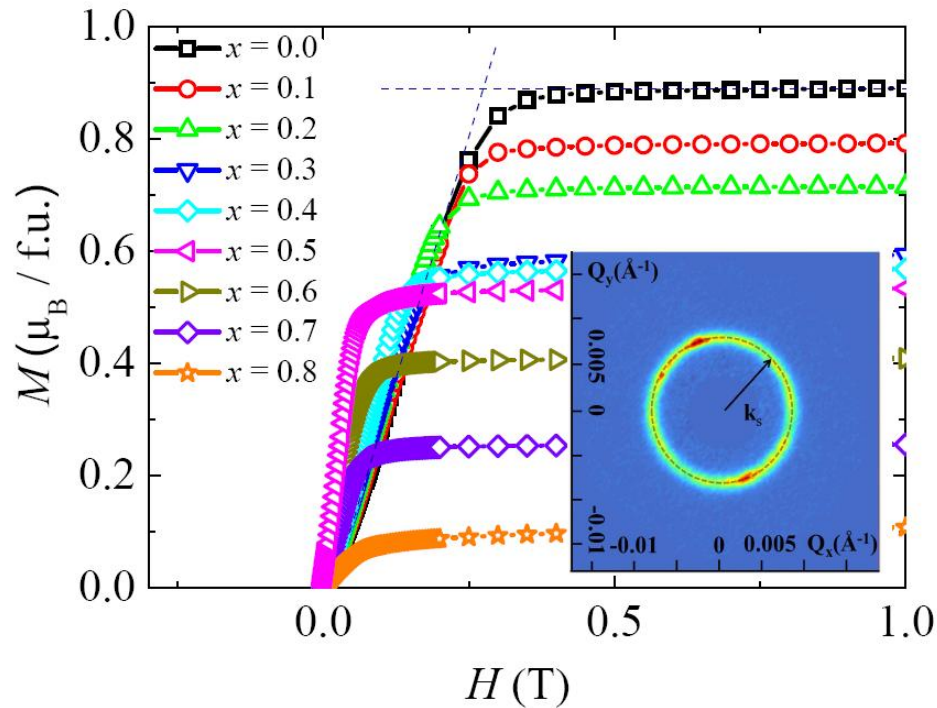
**Left-handed
helix**



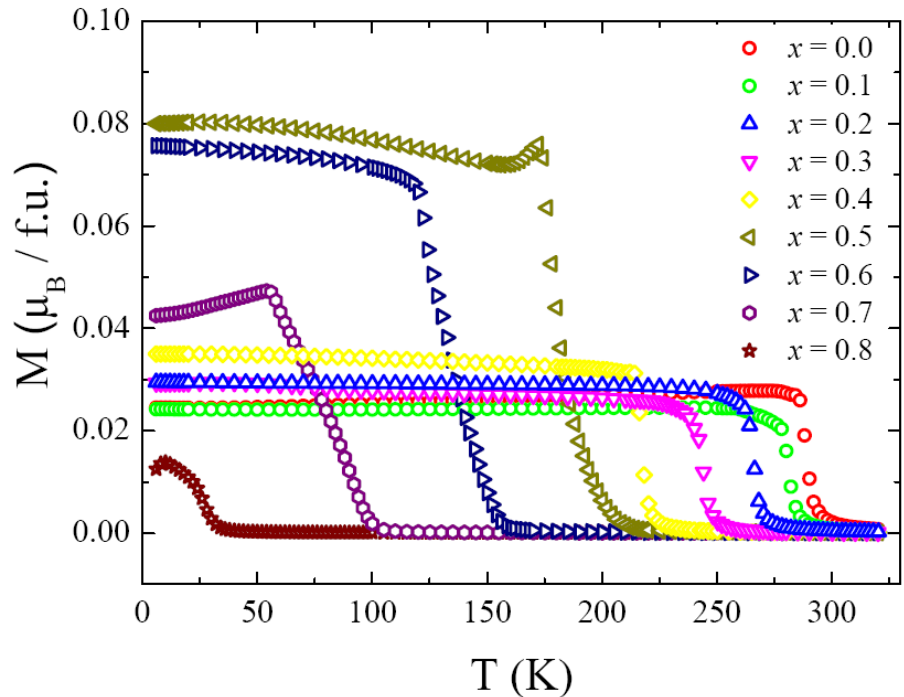
Characteristic parameters:

T_C , S , k , H_{C1} , H_{C2}

Magnetic ordering in $\text{Fe}_{1-x}\text{Co}_x\text{Ge}$

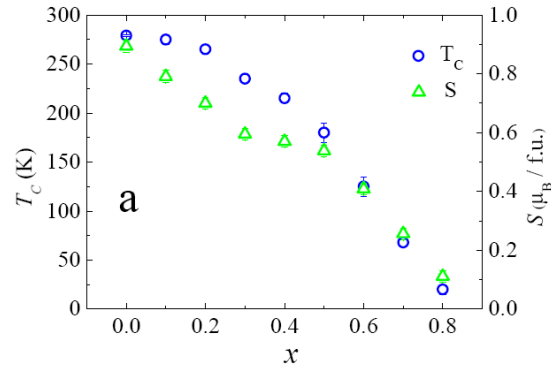


Samples: $\text{Fe}_{1-y}\text{Co}_y\text{Ge}$ (0,0.1... -.. 1.0)
 (A.V. Tsvyashchenko,
 Institute for High Pressure
 Physics, Troitsk, Russia)



Susceptibility measurements

Critical temperature T_C , spiral wavevector k and critical fields in $\text{Fe}_{1-x}\text{Co}_x\text{Ge}$

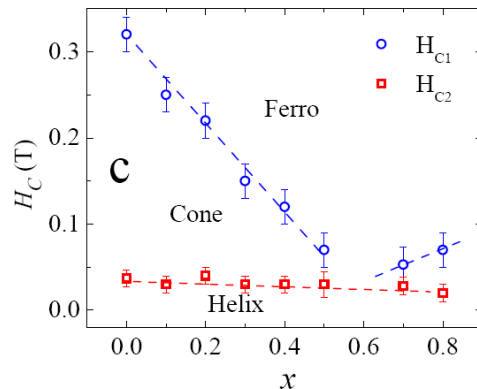
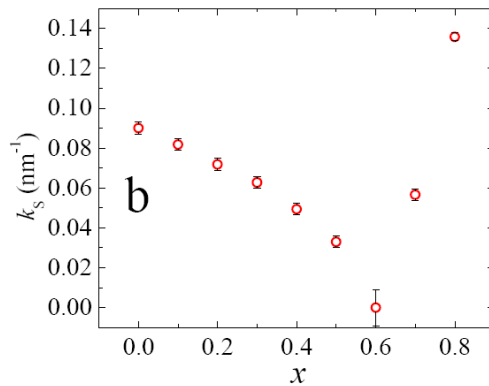


Characteristic parameters: T_C , S , k , H_{C1} , H_{C2}

1) $A k^2 = g \mu_B H_{C2}$ критическое поле перехода в ферромагнитную фазу

2) $k = D / J$ волновой вектор спирали

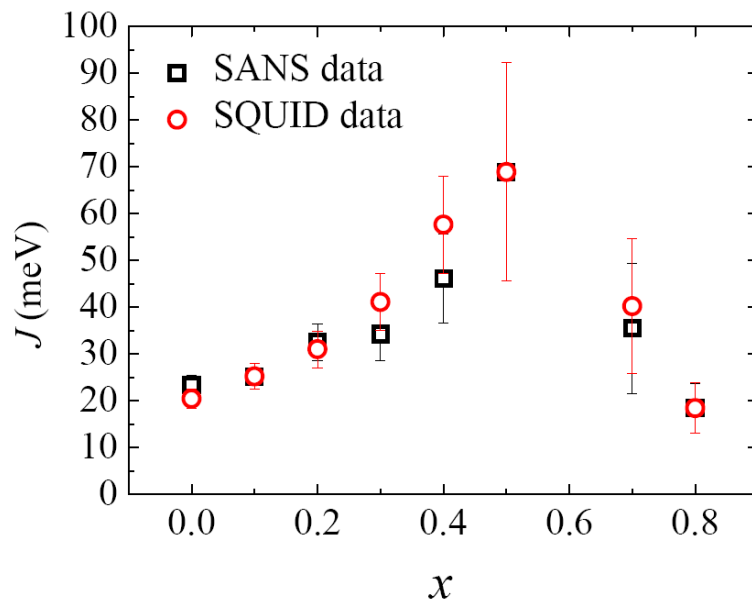
3) $J = A / S$



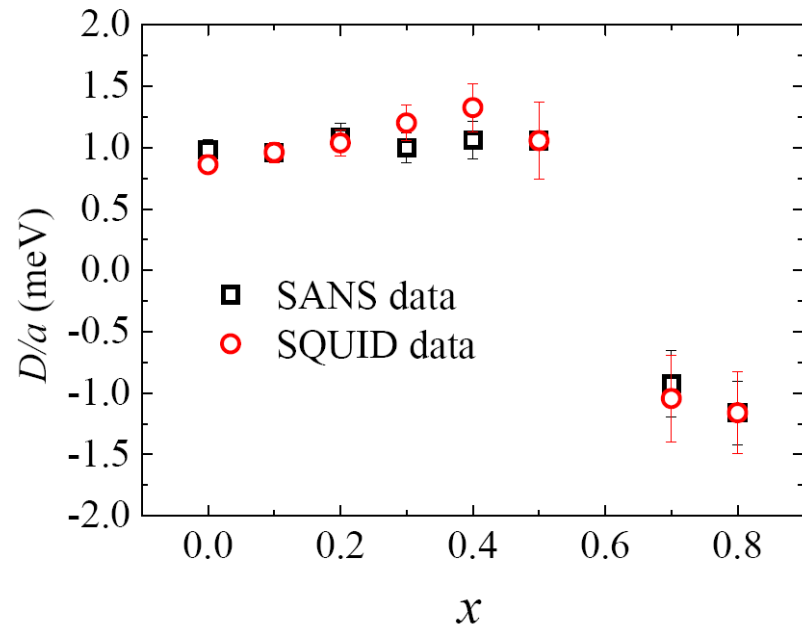
The wavevector $k = 0$, $T_C = 140$ K

The system transforms to ferromagnet

Driving interactions of the magnetic system



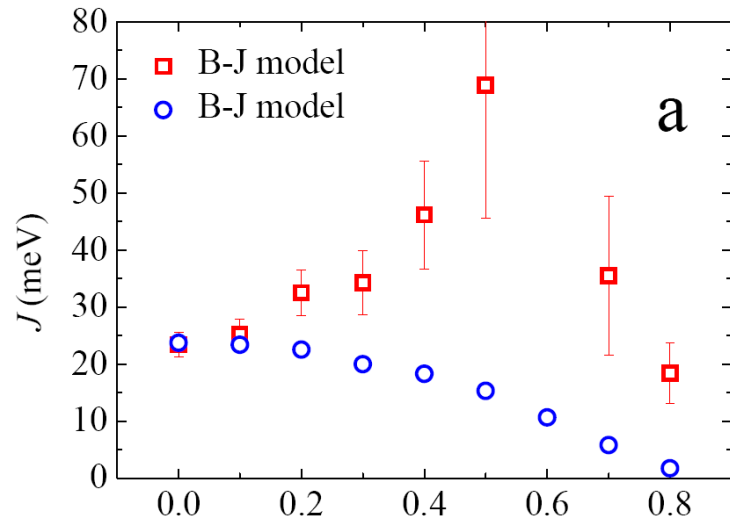
$$J = A/S = g \mu_B H_{C2} / S k^2$$



$$D/a = J k/a$$

The “chiral catastrophe” of B-J model

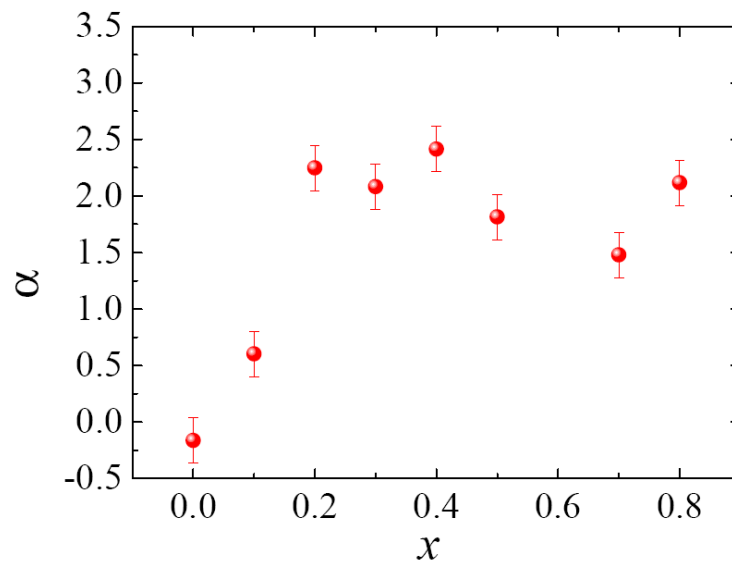
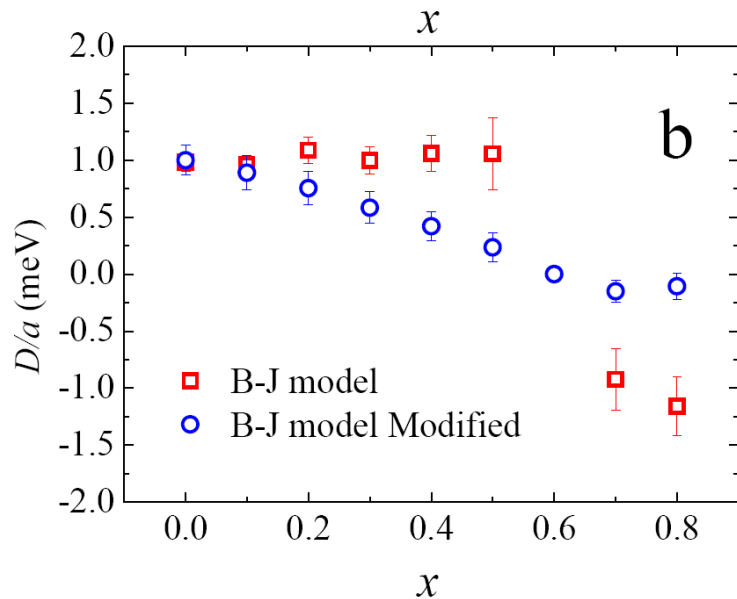
Different approach to treat data



1) $J = k_B T_C$ and $A = S J$

2) $k = D / J$

3) $g \mu_B H_{C2} = A k^2 + a g \mu_B H_{C1}$



Conclusion

- Thus, we show experimentally that the value of H_{C2} has the minimal value of $2H_{C1}$ and that the cubic anisotropy plays an important role in the compounds, where the wave vector k becomes relatively low.
- The theoretical consideration below approves the experimental findings.

Non-CentroSymmetric Magnets (NCSM)

In NCSM Dzyaloshinskii-Moriya interaction (DMI) is allowed between any spin pairs.

It is linear in the spin-orbit interaction and it is the strongest anisotropic interaction.

As was recently shown in [1,2] one can change average value of DMI by mixing magnetic ions.

[1] S. V. Grigoriev, et al, Phys. Rev. Lett. 110 (2013) 207201.

[2] K. Shibata, et al, Nature Nanotechnology 8, 723-728 (2013).

Bak-Jensen Model in B20 compounds

- Cubic symmetry;
- Interactions: Exchange; DMI, Zeeman.
- Assumption: Helical structure.

$$\mathbf{S}_{\mathbf{R}} = S[\hat{c} \sin \alpha + (\mathbf{A} e^{i\mathbf{k} \cdot \mathbf{R}} + A^* e^{-i\mathbf{k} \cdot \mathbf{R}}) \cos \alpha]$$

where $\mathbf{k}$ is the helix wave-vector.

$$\mathbf{A} = (\hat{a} - i\hat{b})/2,$$

$[\hat{a} \times \hat{b}] = \hat{c}$ determines the spin rotation plane.

α is the cone angle:

if $\alpha = 0$ we have a plane helix and

if $\alpha = \pi/2$ we have ferromagnet.

Result of B-J model

The helix has lower energy than the ferromagnet.

$$E_{BJ} = [SAk^2 - S^2D(\mathbf{k} \cdot \hat{c})] \cos^2 \alpha + H \sin \alpha$$

where A and D are the spin-wave stiffness and DMI constant.

E_{BJ} is minimal if

$$\mathbf{k} = (SD/A)\hat{c}; \quad \sin \alpha = -H/H_c,$$

here $H = H_{\parallel}$ is the field component along $\hat{c}$ and $H_c = Ak^2$ is the critical field for ferromagnetic transition.

Cubic Anisotropy

- In each lattice point

$$E_{CA} = K(S_x^4 + S_y^4 + S_z^4) = G \begin{cases} 1; \mathbf{S} \parallel (1, 0, 0), \\ 1/3; \mathbf{S} \parallel (1, 1, 1). \end{cases}$$

$$G = KS^4; \quad K > 0, \mathbf{S} \parallel (1, 1, 1); \quad K < 0, \mathbf{S} \parallel (0, 0, 1)$$

DMI Helix in Cubic Crystals

Interactions - Exchange DM and Zeemann - are isotropic. So the helix energy

$$E = -(SAk^2/2) \cos^2 \alpha + G[C \sin^4 \alpha + (3/8)B \cos^4 \alpha + 3I \sin^2 \alpha \cos^2 \alpha] + SH_{\parallel} \sin \alpha,$$

The cubic invariants C , B , I are given by

$$C = \sum \hat{c}_j^4; B = \sum (\hat{a}_j^2 + \hat{b}_j^2)^2; I = \sum \hat{c}_j^2 (\hat{a}_j^2 + \hat{b}_j^2)$$

Extremal values:

$$C = 1, B = 2; I = 0; \hat{c} = (0, 0, 1);$$

$$C = 1/3, B = 4/3; I = 2/3; \hat{c} = (1, 1, 1)/\sqrt{3}$$

Equilibrium Conditions

$G > 0$. Results for $G < 0$ are very similar.

The first condition: Extreme values of invariants C, B and I . The field is along $(1,1,1)$. The energy

$$E = (-Ak^2 + G)/2 + (Ak^2/2 + G) \sin^2 \alpha - (7/6) \sin^4 \alpha + H \sin \alpha,$$

and its minimum condition:

$$[Ak^2 + 2G - (14G/3) \sin^2 \alpha] \sin \alpha = -H,$$

Final Results I.

- Zero field $H=0$, $\bar{A}k^2 > G/3$
- Planar helix-->Ferromagnet.
- Strong DMI: $Ak^2 > 12G$; $g = (Ak^2/G + 2)/14$:
- Ferromagnetic transition
 $\sin \alpha_c = -1$; $Ak^2 > H_c = AK^2 - 8G/3 > 7Ak^2/9$

FINAL RESULTS ii.

- Weak DMI: $1 > g > q > 1/6$;
- ($1/6 > g \rightarrow$ ferromagnet.)
- The conical helix is stable if
$$\sin \alpha > -\sqrt{g} > -1$$
- The first order transition to ferromagnet determined by two conditions:
- Energy minimum
- Equality
Conical energy=ferromagnetic=G/3-H.

Final Equations

- Line of transitions

$$28G\sqrt{g/3} > H' > 0; \quad -1 < \sin \alpha < 0$$

determined by

$$\left(g - \frac{\sin^2 \alpha}{3}\right) \sin \alpha = H/14G$$

$$\sin^2 \alpha = g - \sqrt{(g+1)^2 - 4/3} - \frac{2H}{7G}$$

Conclusion

- B20 magnets have very complex field behavior. The same holds for other NCSM due to DMI.
- At present we have very poor understanding corresponding phenomena.
- Their study is one of the urgent tasks in magnetism.

THANK YOU