



# Совещание по использованию рассеяния нейтронов и синхротронного излучения в конденсированных средах



## *Эффект нейтронного гетеродинирования и быстрая кинетика нано-систем*

**Б.П. Топерверг**

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Национального исследовательского центра «Курчатовский институт»

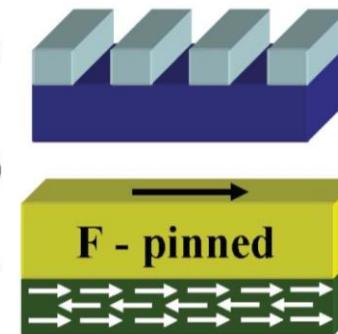
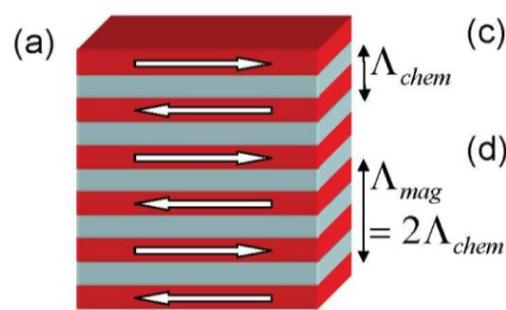
# *Collaborators*

- Kirill Zhernenkov (CEA-Grenoble)
- Dima Gorkov (Ruhr Uni-Bochum)
- Sergey Klimko (LLB Saclay)
- Nicolas Martin (TU München & LLB)
- Louis-Pierre Regnault (CEA-Grenoble)
- Roland Gähler (ILL-Grenoble)
- Hartmut Zabel (Ruhr Uni-Bochum)

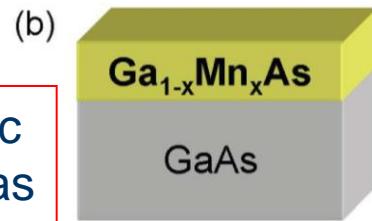
# Where the spins are and what they are doing in nano-materials.

## Current subjects for reflectometry:

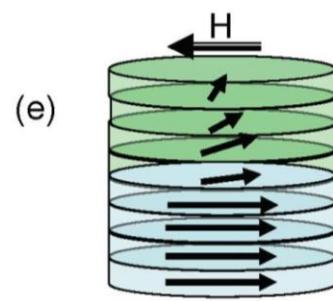
a) Exchange coupled bi-layers and superlattice with antiferromagnetic ordering  
**(GMR and TMR systems)**



c) Laterally patterned magnetic films, **nano-wires**,etc.



b) Dilute magnetic semiconductors as **spin-injectors** in semiconductor heterostructures



d) Ferromagnetic films on antiferromagnetic substrates with **Exchange bias** through common interfaces

e) **Spring magnets**: soft magnetic layer exchange coupled to a magnetically hard layer (spin valves)

Also: Superconducting films, polymer films, membranes, etc

# *Recent Review Articles*

H. Zabel, K. Theis-Bröhl, B.P. Toperverg,

**“Polarized neutron reflectivity and scattering of magnetic nanostructures  
and spintronic materials”**

*Handbook of Magnetism and Advanced Magnetic Materials,*

H. Kronmüller & S. Parkin (Eds.), NY, Wiley 2007, pp. 1237-1288

A. Remhof, A. Westphalen, K. Theis-Bröhl, J. Grabis, A. Nefedov,  
B. Toperverg, H. Zabel

**“Magnetization Reversal Studies of Periodic Magnetic Arrays via  
Scattering Methods”**

*Springer Series in materials science 94, Springer-Verlag Berlin Heidelberg 2007 pp.65 - 97*

H.-J.C. Lauter, V. Lauter, B.P. Toperverg

**“Reflectivity, Off-Specular Scattering, and GI-SAS: Neutrons”**

*Polymer Science: A Comprehensive Reference, Vol 2, pp. 411–432 (2012)*

Matyjaszewski K & Möller M (eds.) Amsterdam: Elsevier BV

M.R. Fitzsimmons & I.K. Schuller

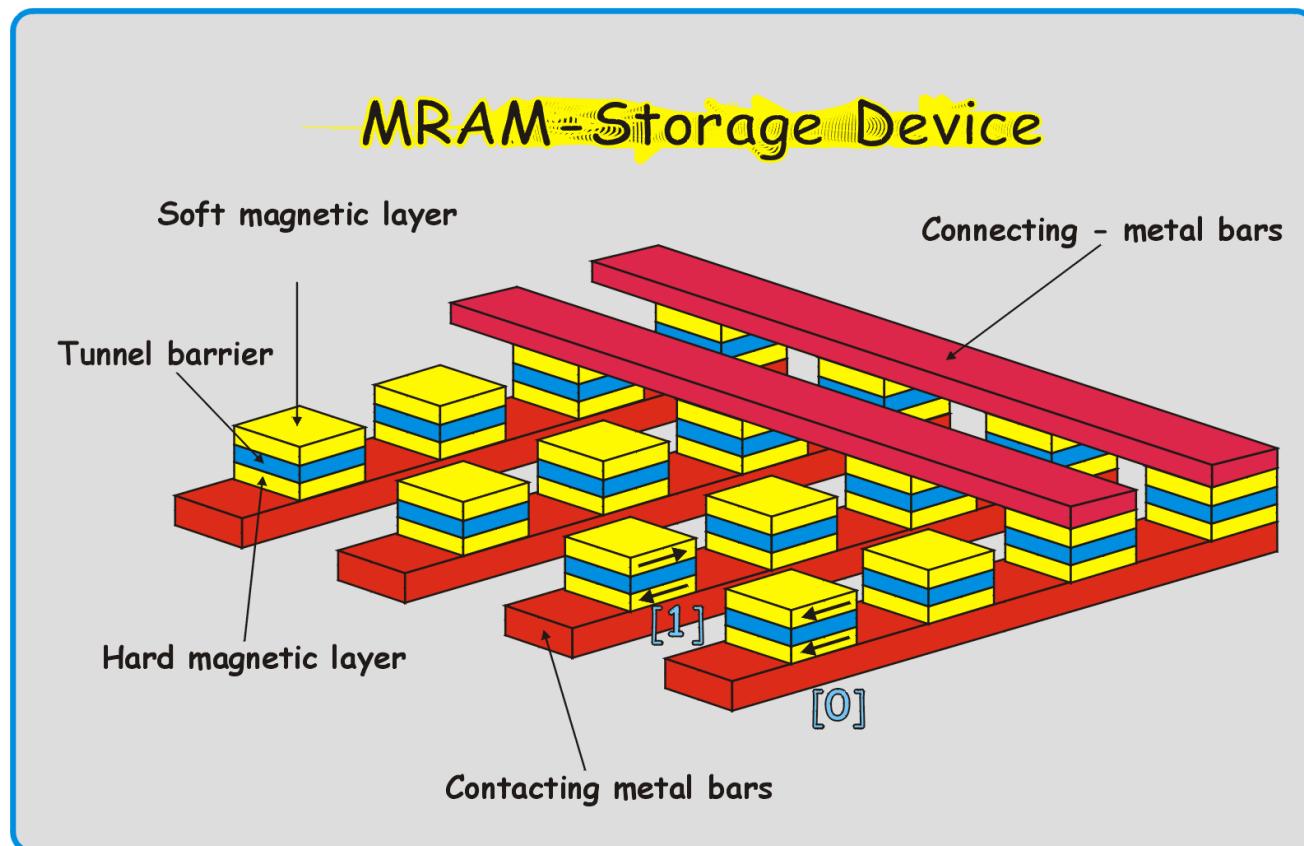
**“Neutron scattering – The key characterization tool for nanostructured magnetic materials ”**

*JMMM, 350 (2014) 199-208*

# To-day spintronic material application: Magnetic Random Access Memory (MRAM)

- → “read-write” 2D arrays of spin valves
  - Writing with weak magnetic field
  - Reading with electric current

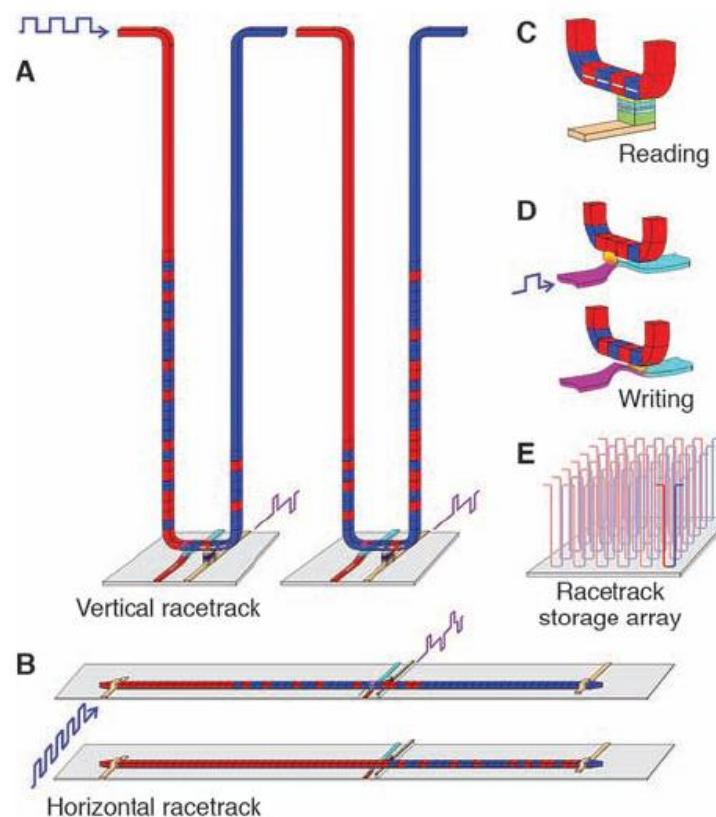
**Neutrons:**  
**Intrinsic mechanisms and rates of spin rearrangement in nano-elements and their ensembles**



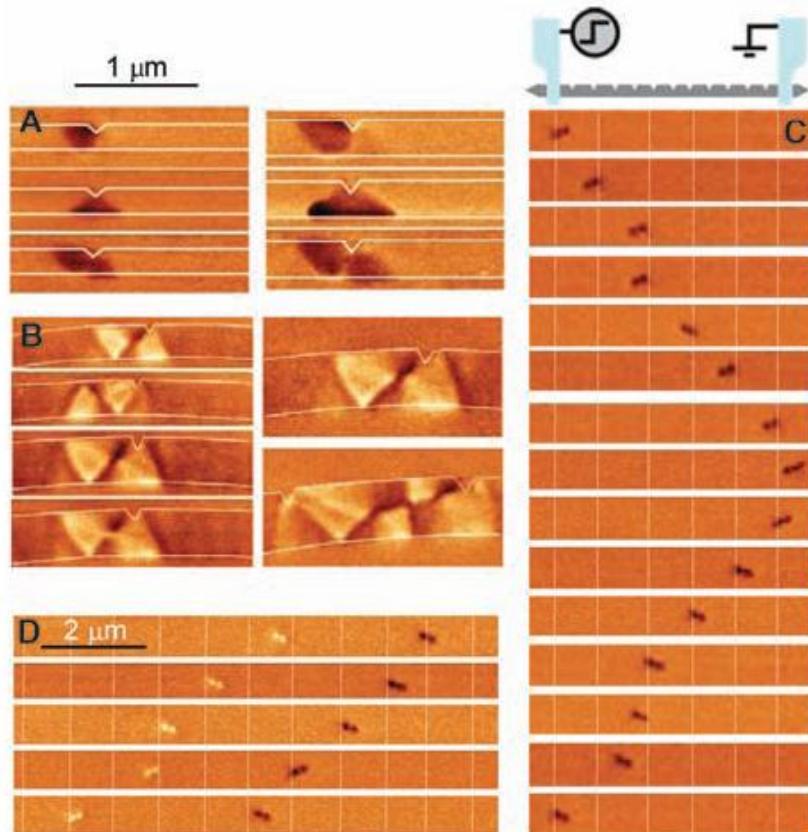
## Emerging Challenges: non-linear spin dynamics & kinetics

# Magnetic Domain-Wall Racetrack Memory

Stuart S. P. Parkin,\* Masamitsu Hayashi, Luc Thomas



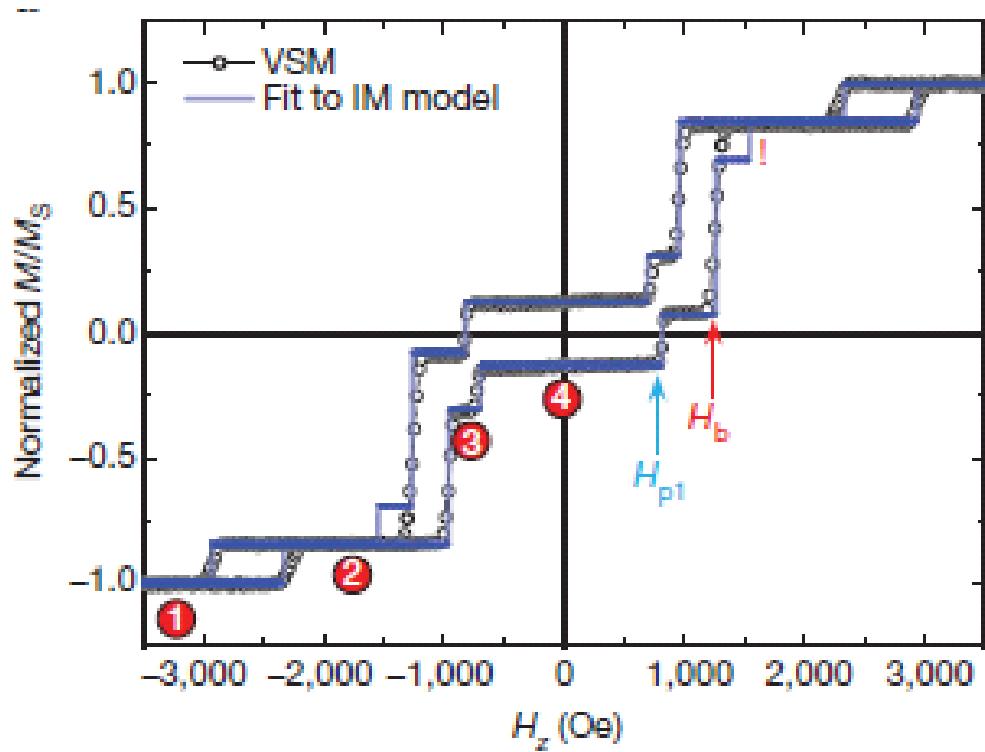
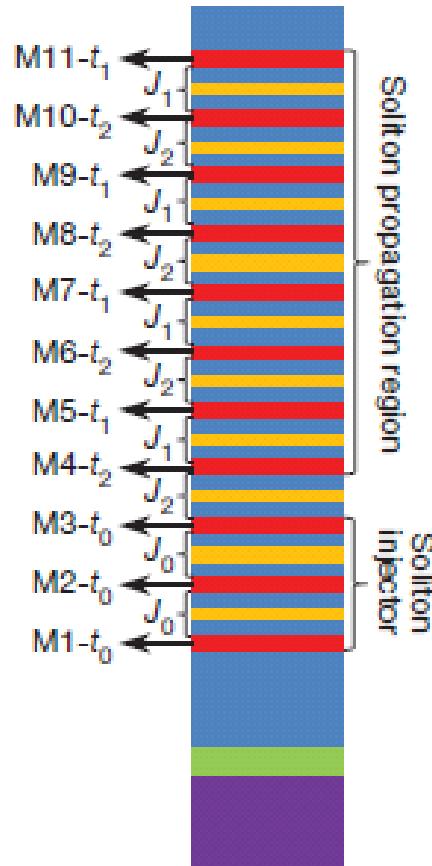
11 APRIL 2008 VOL 320 SCIENCE



# Magnetic ratchet for three-dimensional spintronic memory and logic

Reinoud Lavrijsen<sup>1</sup>, Ji-Hyun Lee<sup>1</sup>, Amilio Fernández-Pacheco<sup>1</sup>, Dorothée C. M. C. Petit<sup>1</sup>, Rhodri Mansell<sup>1</sup> & Russell P. Cowburn<sup>1</sup>

31 JANUARY 2013 | VOL 493 | NATURE | 649



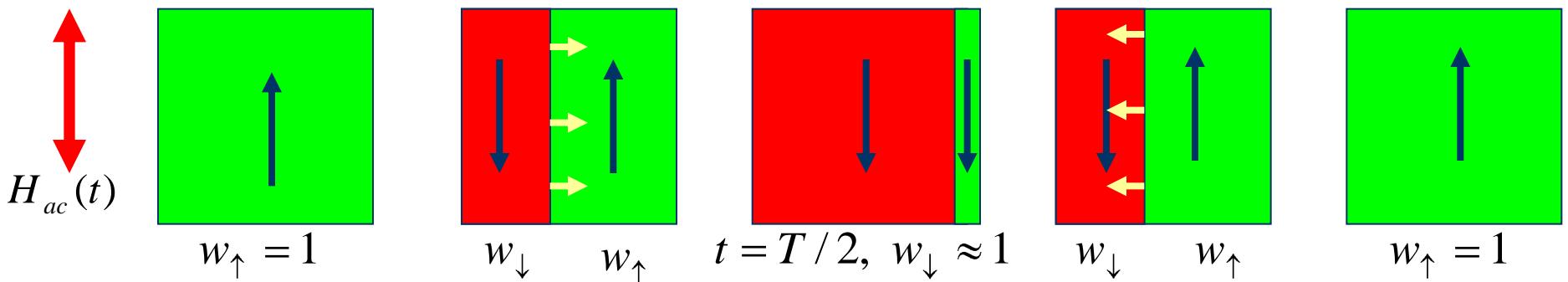
Layer-by-layer *time resolved* magnetometry with PNR?

## Frequency dependence of magnetization reversal in thin Fe(100) films

K. Zhernenkov,<sup>1,\*</sup> D. Gorkov,<sup>1</sup> B. P. Toperverg,<sup>1,2</sup> and H. Zabel<sup>1</sup>

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<sup>2</sup>*Petersburg Nuclear Physics Institute, 188300 Gatchina, Russia*



Reduced magnetization  $m(t) = M(t)/M_{\text{sat}} = w_{\uparrow} - w_{\downarrow} = 1 - 2w_{\downarrow}(t)$ ,

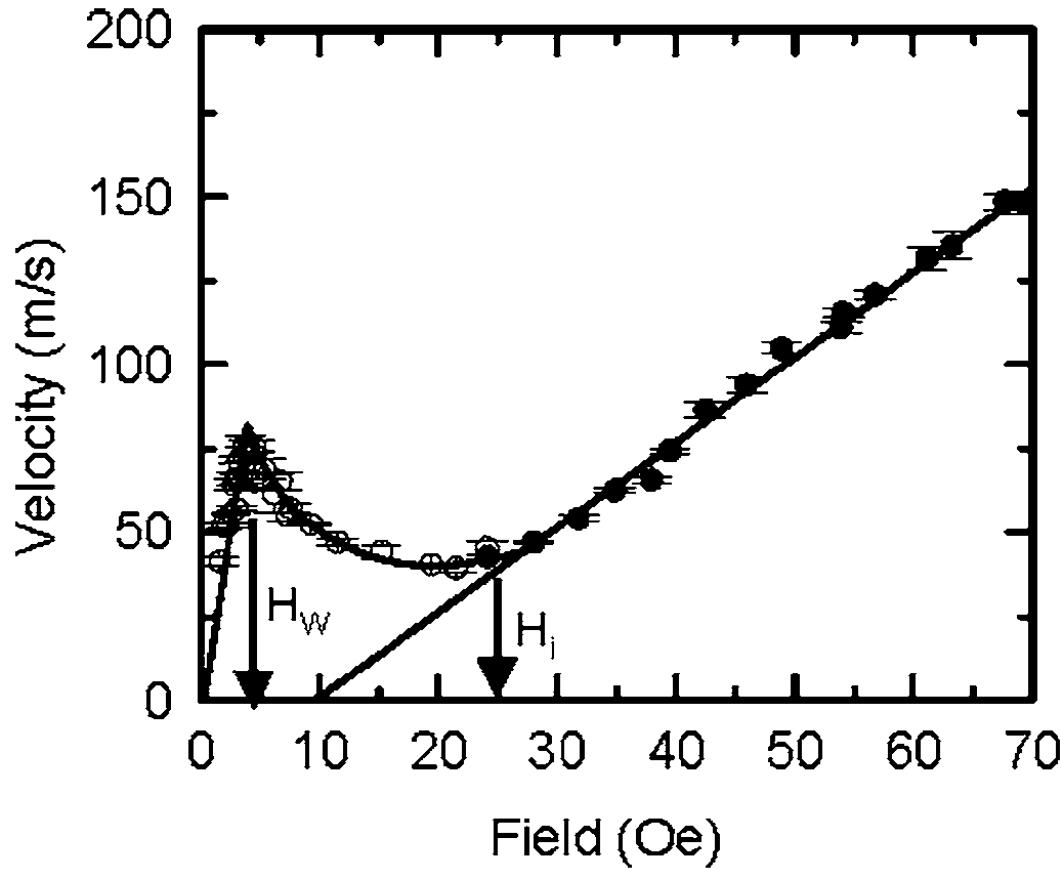
Surface fraction  $w_{\downarrow}(t) = \frac{1}{l} \int_0^t dt' v(t')$  with negative magnitization ,  $l$  is domain size

$v(t) = \mu_{\text{DW}} H(t)$  is DW velocity (Landau & Lifshits, 1935),  $\mu_{\text{DW}}$  is DW mobility

If  $H(t) = H_0 \sin(\omega \cdot t)$  then  $w_{\downarrow}(t) = \mu_{\text{DW}} H_0 \frac{1 - \cos(\omega \cdot t)}{\omega \cdot l}$ ,

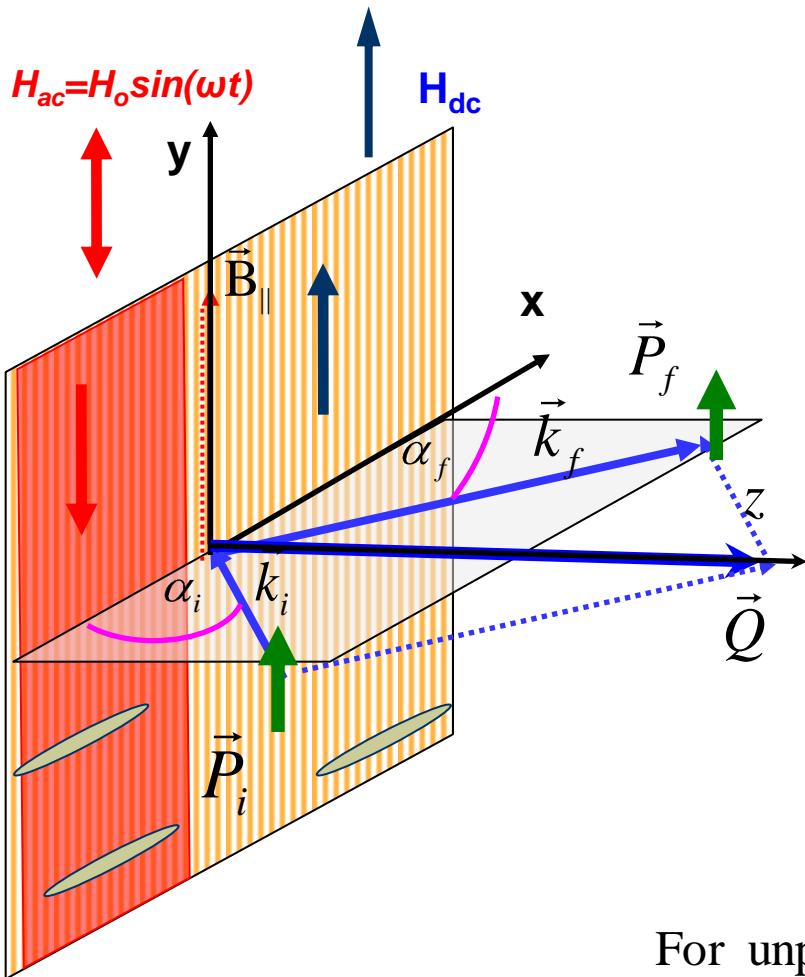
$m(t) = \bar{m} + \Delta m(t)$ , where  $\bar{m} = 1 - 2\mu_{\text{DW}} H_0 \frac{1}{\omega \cdot l}$ ,  $\Delta m(t) = 2\mu_{\text{DW}} H_0 \frac{\cos(\omega \cdot t)}{\omega \cdot l}$

# Landau-Lifshits regime vs Walker break down



Schyer & Walker, 1974

# Reflection for polarization collinear with magnetization



## Reflection coefficients (ideal polarization, no analysis)

$$R(\vec{b}) = \frac{1}{2} = |R_+|^2 \cdot [ + (\vec{P} \cdot \vec{b}) ] |R_-|^2 \cdot [ - (\vec{P} \cdot \vec{b}) ]$$

$R_{\pm}$  are reflection amplitudes for  $\pm$  spin states

Surface average for time moment  $t$ :

$$R = w_{\uparrow} R(\vec{b}) + w_{\downarrow} R(-\vec{b}), \quad \vec{b} = \vec{B}_{\parallel} / |\vec{B}_{\parallel}|$$

$$R^+(t) = \frac{1}{2} |R_+|^2 \cdot [ + m(t) ] |R_-|^2 \cdot [ - m(t) ]$$

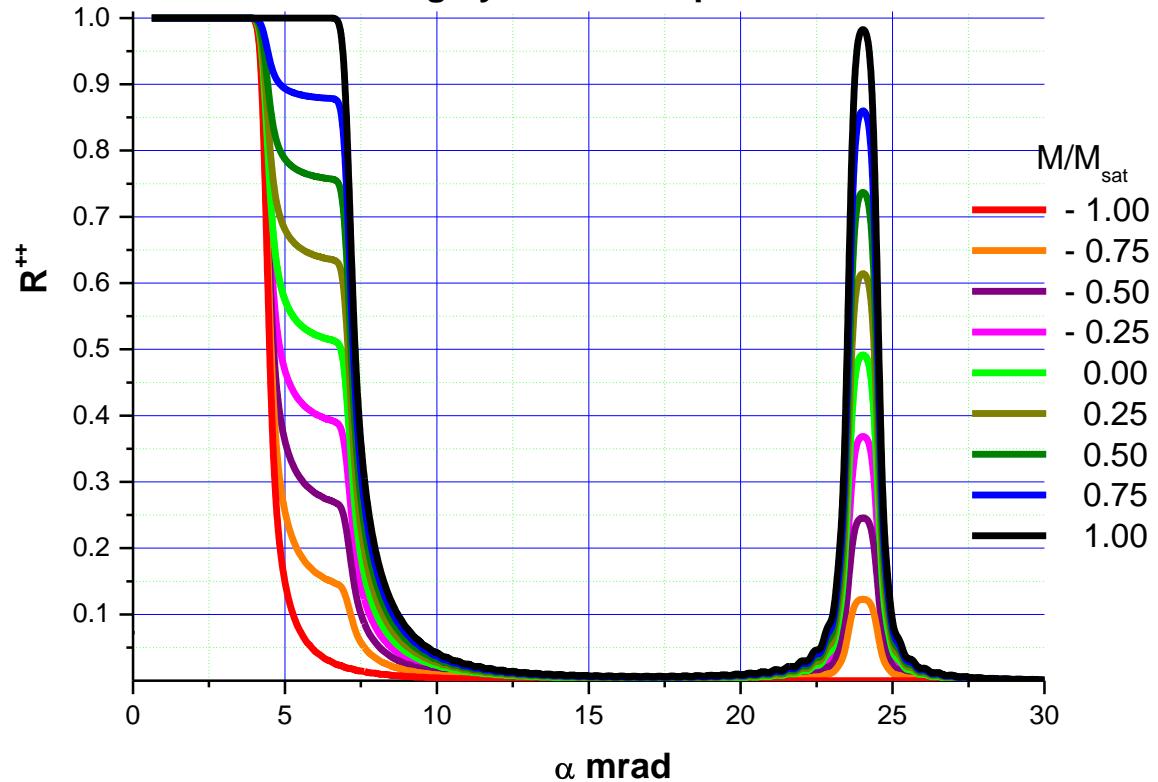
$$R^-(t) = \frac{1}{2} |R_+|^2 \cdot [ - m(t) ] |R_-|^2 \cdot [ + m(t) ]$$

For unpolarized beam  $R = \frac{1}{2} |R_+|^2 + |R_-|^2$  } no effect

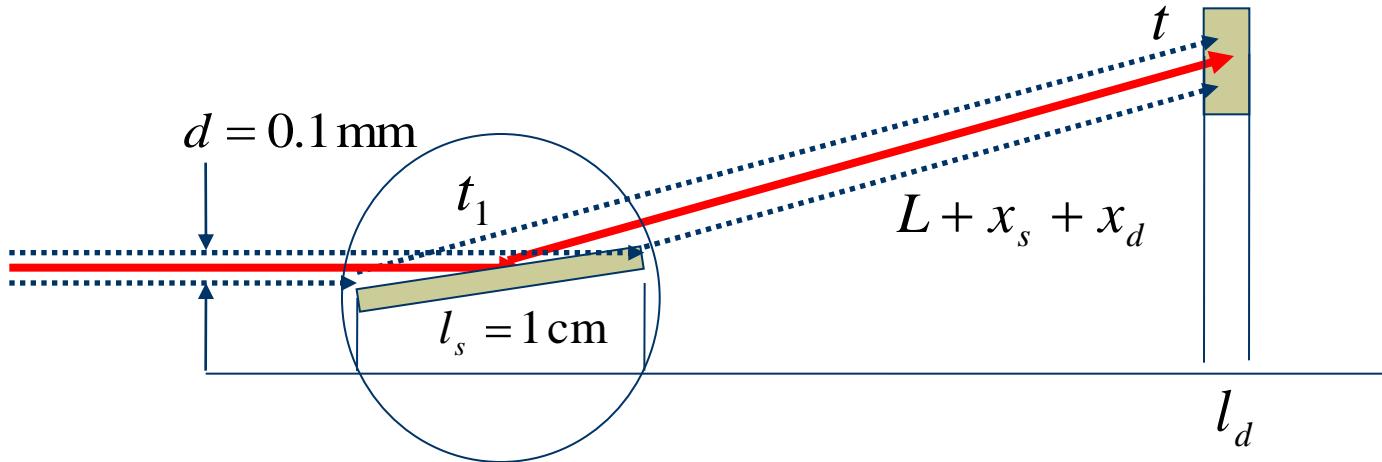
For ideal mirror,  $|R_+| = 1, |R_-| = 0$ , and  $H(t) = H_0 \sin(\omega \cdot t)$

the reflected intensity is modulated as :  $R = \frac{\mu_{DW} H_0}{\omega \cdot l} [- \cos(\omega \cdot t)]$

**Simulated  $R^+$  reflectivities for [Fe/Si]x50 polarizing Bragg mirror  
along hysteresis loop**



## Time modulation and smearing of PNR response



$$I(t) = R_0 + \frac{1}{l_s} \int_{-l_s/2}^{l_s/2} dx_s \frac{1}{l_d} \int_{-l_d/2}^{l_d/2} dx_d \int d\lambda R_p \cos\{\omega \cdot [t - (L + x_s + x_d)/v_n]\} \cdot W(\lambda)$$

$$v_n = 1/c\lambda, \quad c = (m_n / 2\pi\hbar) = 0.2528 \cdot 10^{-5} \text{ sec}/(\text{cm} \cdot \text{\AA}), \quad t = \bar{t} + \Delta t, \quad \bar{t} = c\lambda L,$$

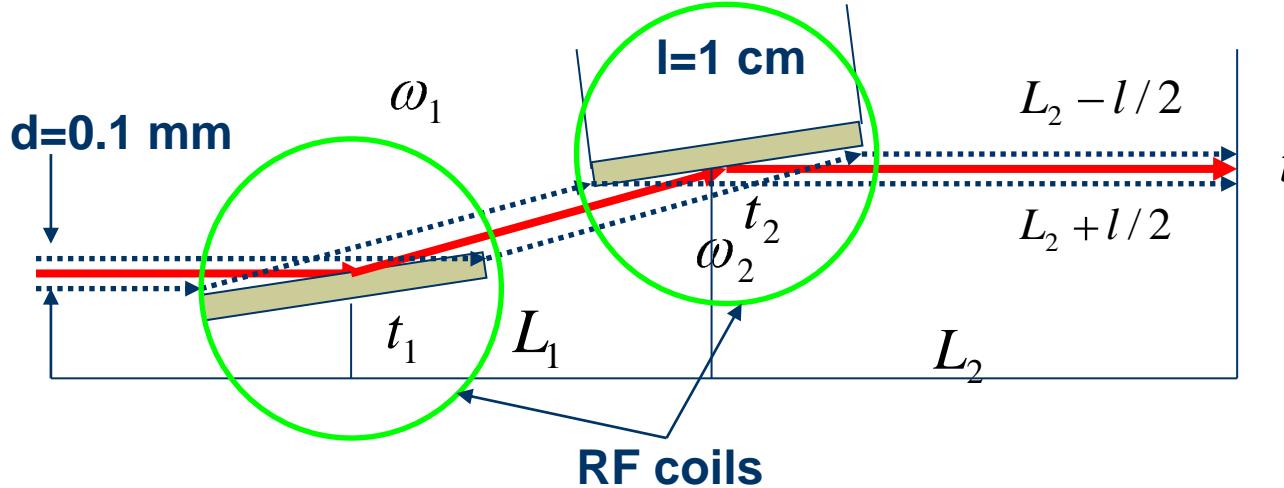
where  $v_n$  is neutron velocity, and  $W(\lambda)$  is spectral function

$(\Delta t / \bar{t}) = \pm (l / L) \pm (\Delta \lambda / \lambda)$  uncertainty in time,

If  $\lambda = 4 \text{ \AA}$ ,  $L = 100 \text{ cm}$ ,  $l = 1 \text{ cm}$ ,  $\Delta \lambda / \lambda = 1\%$ , then  $\bar{t} \cong 1 \text{ msec}$ ,

$$\Delta t_l = c\lambda l \cong 10 \mu\text{sec}, \quad \Delta t_\lambda \cong 10 \mu\text{sec}, \quad \Delta t \cong 20 \mu\text{sec}, \quad f = 50 \text{ kHz}$$

# Time modulation with double reflection



$$I(t) \propto \frac{1}{l} \int_{-l/2}^{l/2} dx \int d\lambda R_2[t - (L_2 + x)/v_n] \cdot R_1[t - (L_1 + L_2 + x)/v_n] \cdot W_0(\lambda)$$

$$R_1 = R_0 + R_p \cos\{\omega_1[t - (\tau_x + \tau_2)]\}, \quad \tau_x = x/v_n, \quad \tau_2 = L_2/v_n$$

$$R_2 = R_0 + R_p \cos\{\omega_2[t - (\tau_x + \tau_2 + \tau_1)]\}, \quad \tau_1 = L_1/v_n$$

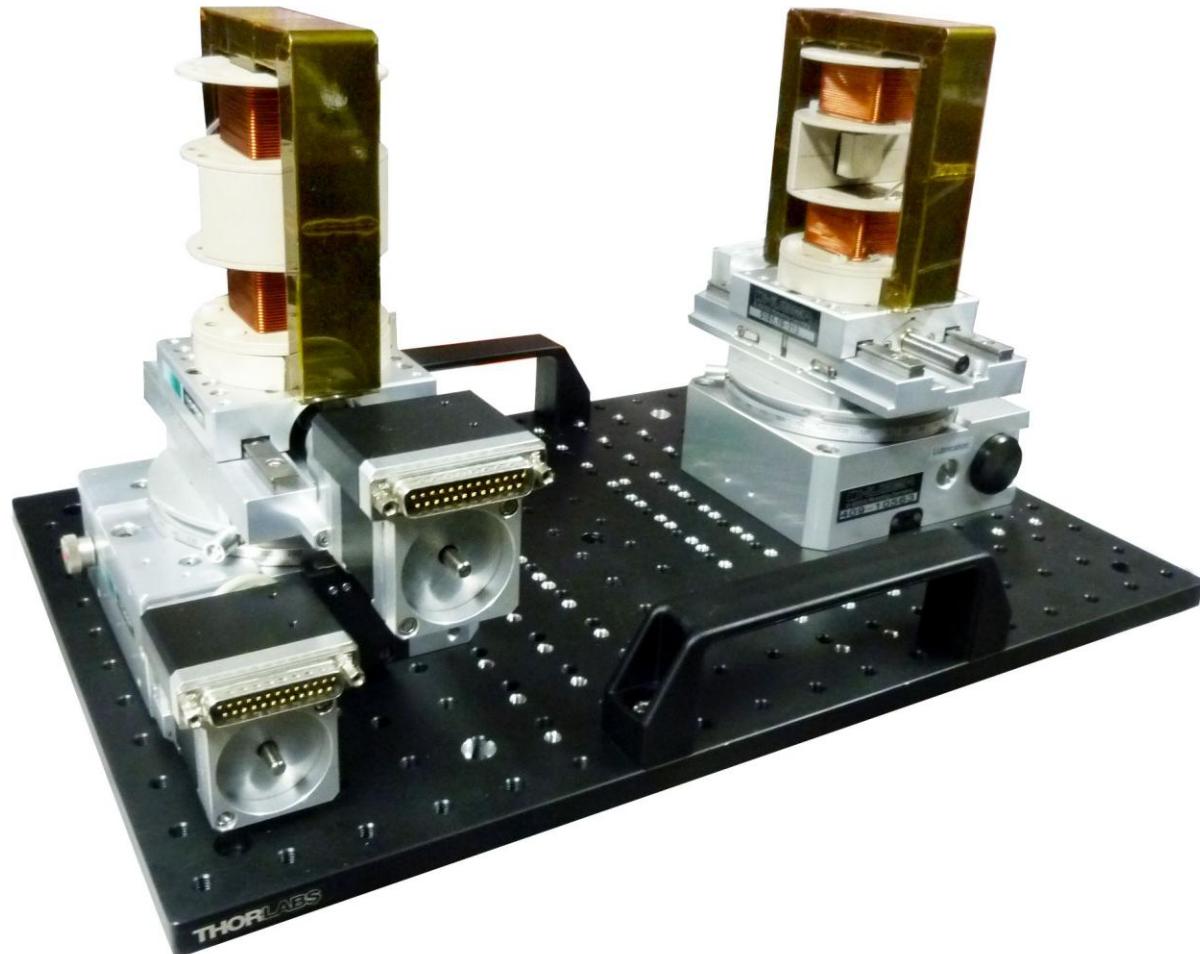
$$\langle \cos\varphi_1 \cdot \cos\varphi_2 \rangle = \frac{1}{2} \langle \cos(\varphi_1 - \varphi_2) + \cos(\varphi_1 + \varphi_2) \rangle \approx \frac{1}{2} \langle \cos(\varphi_1 - \varphi_2) \rangle$$

$$\varphi_1 - \varphi_2 = \omega_H \cdot (t - \tau_x) - [\omega_H \cdot \tau_2 - \omega_1 \tau_1] \approx \omega_H \cdot t - \bar{\phi}$$

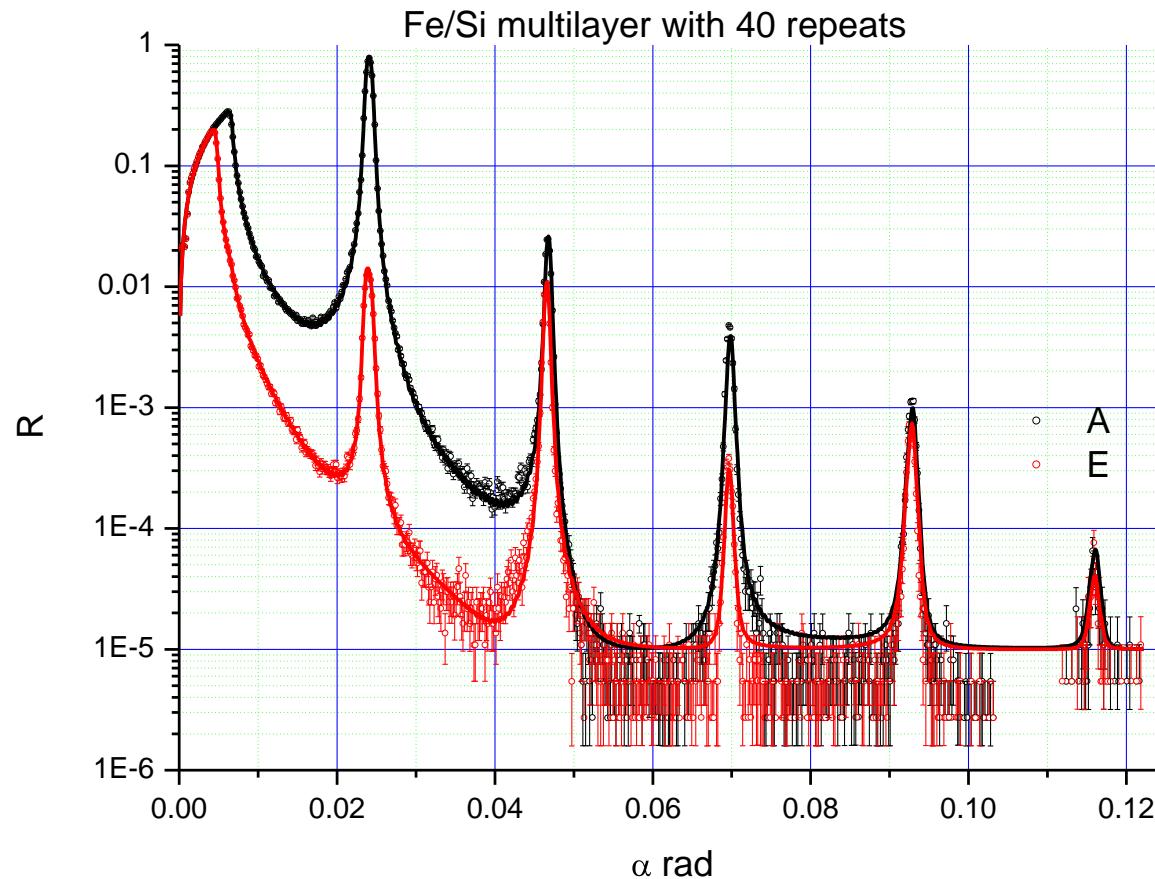
if heterodyne frequency  $\omega_H = \omega_1 - \omega_2$  is small  $\omega_H \tau_x \ll 1$ ,

$$\bar{\phi} = (\omega_H L_2 - \omega_1 L_1)/\bar{v}_n \text{ and at MIEZE conditions } |\omega_H \tau_2 - \omega_1 \tau_1| \ll \Delta\lambda/\bar{\lambda}$$

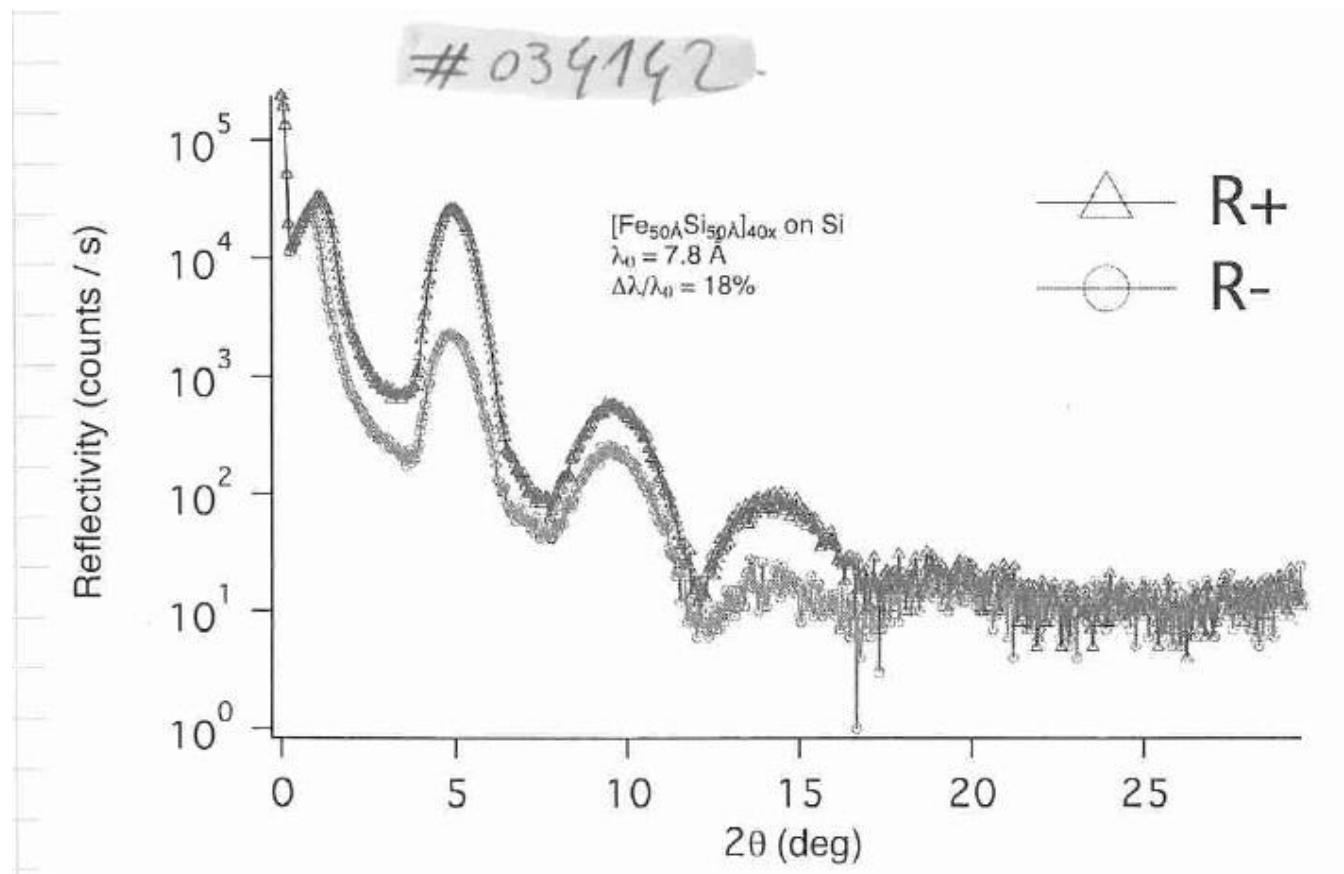
# Heterodyne setup



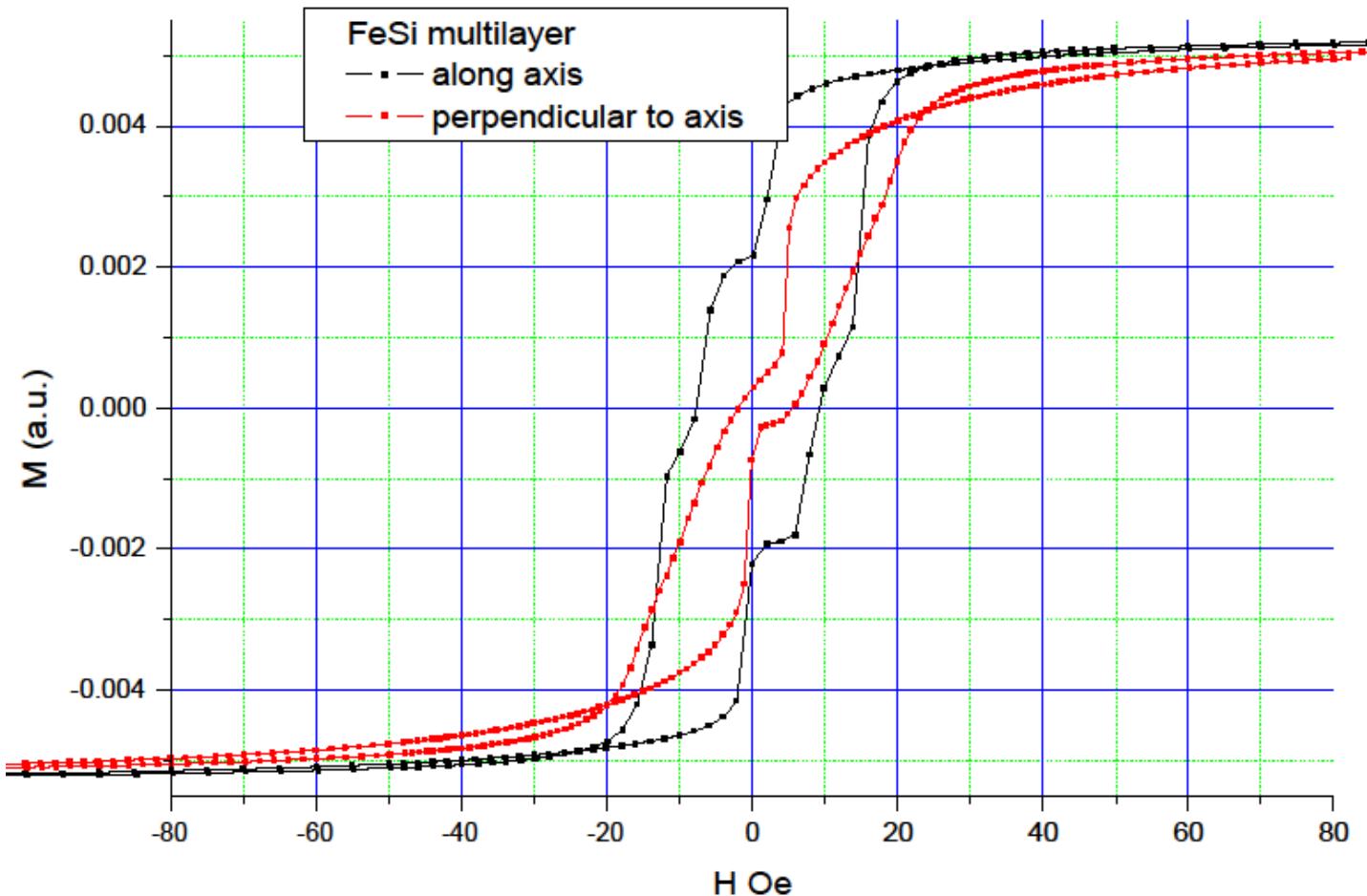
# PNR data (SuperADAM) + fit



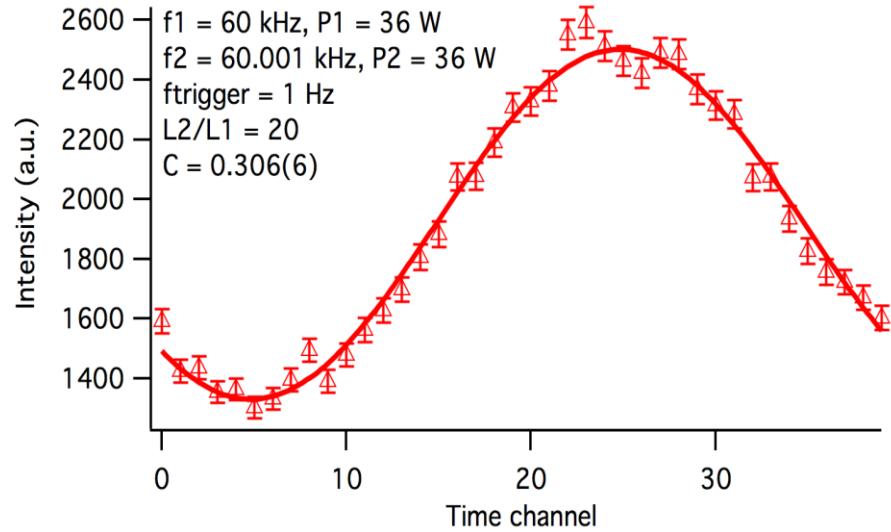
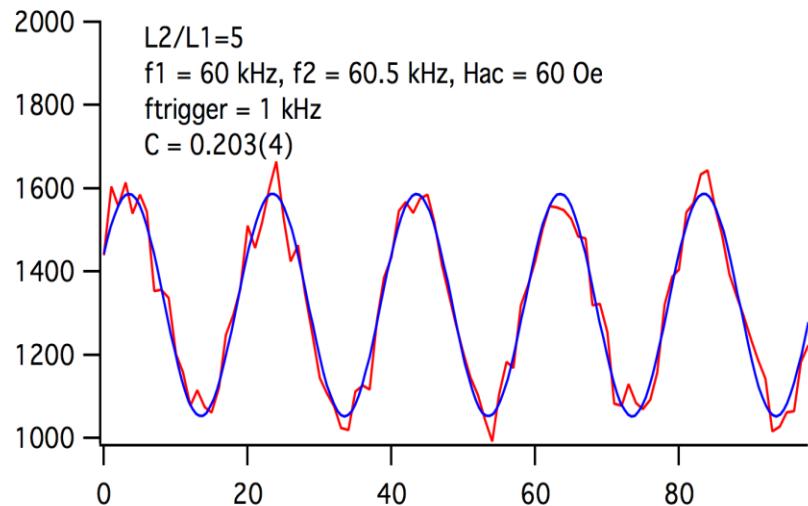
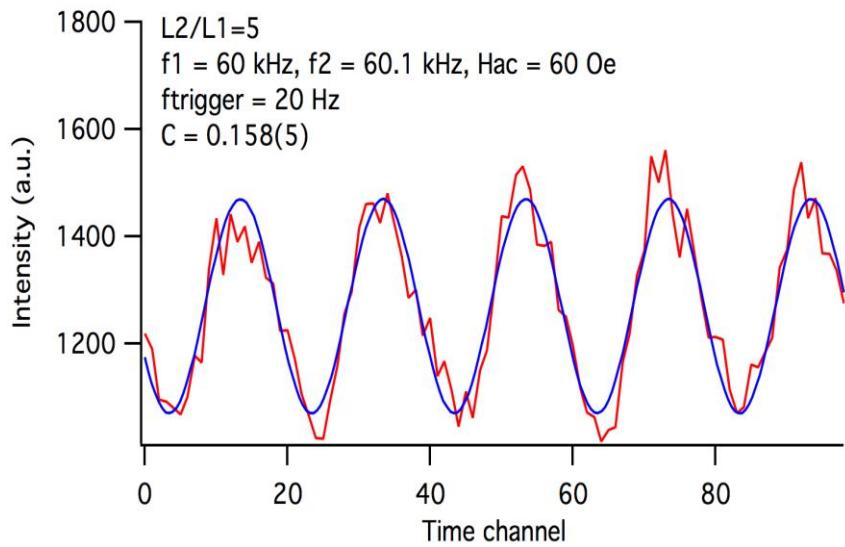
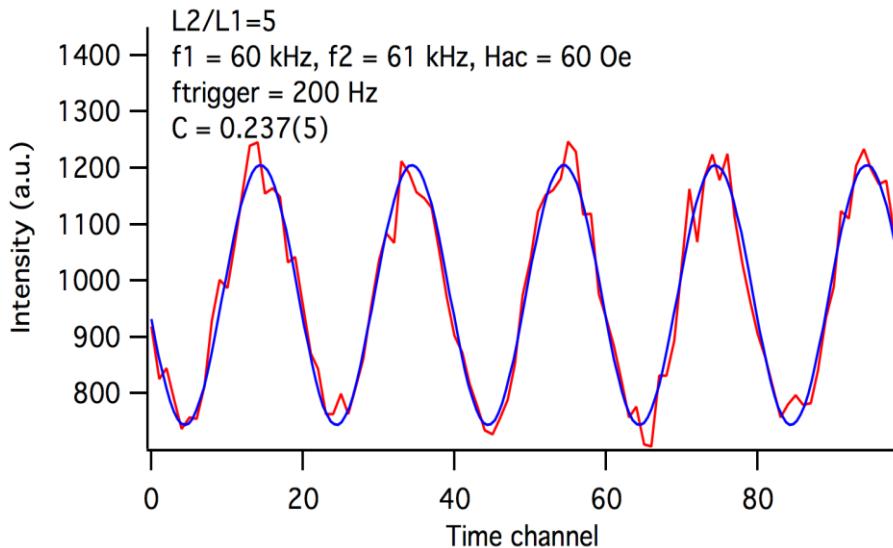
# PNR at RESEDA



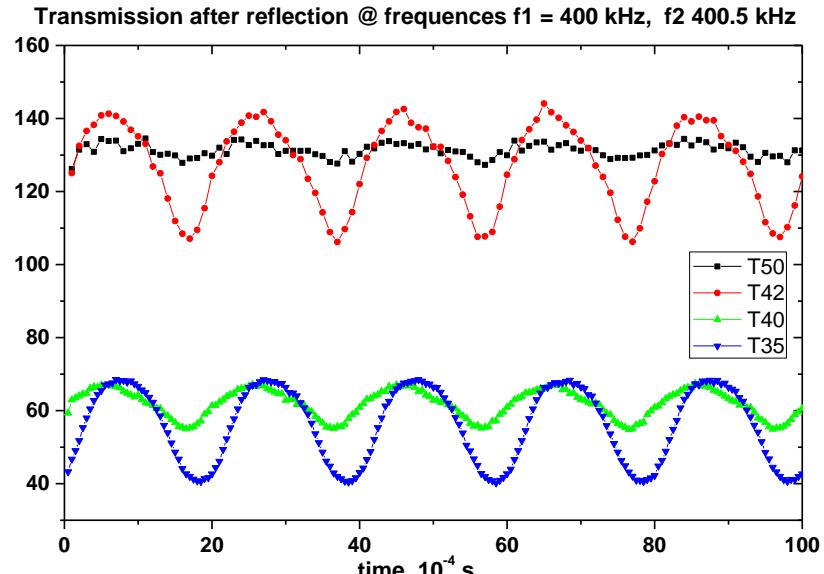
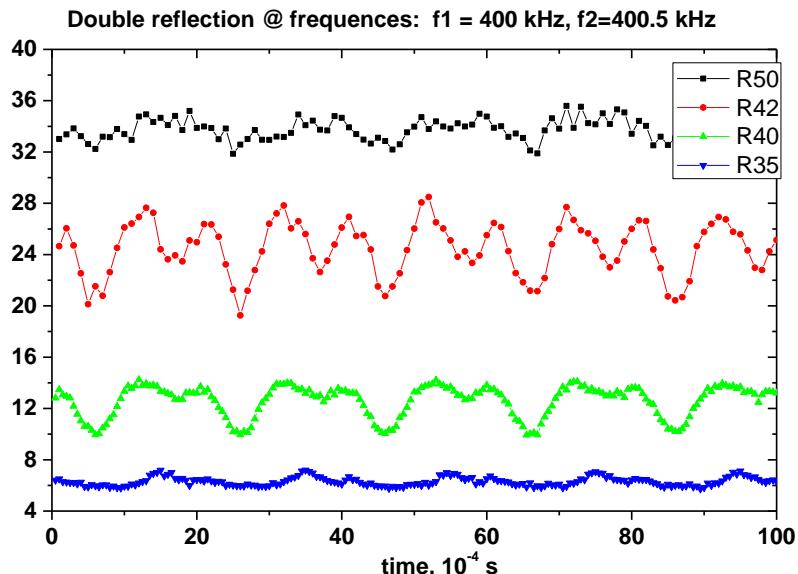
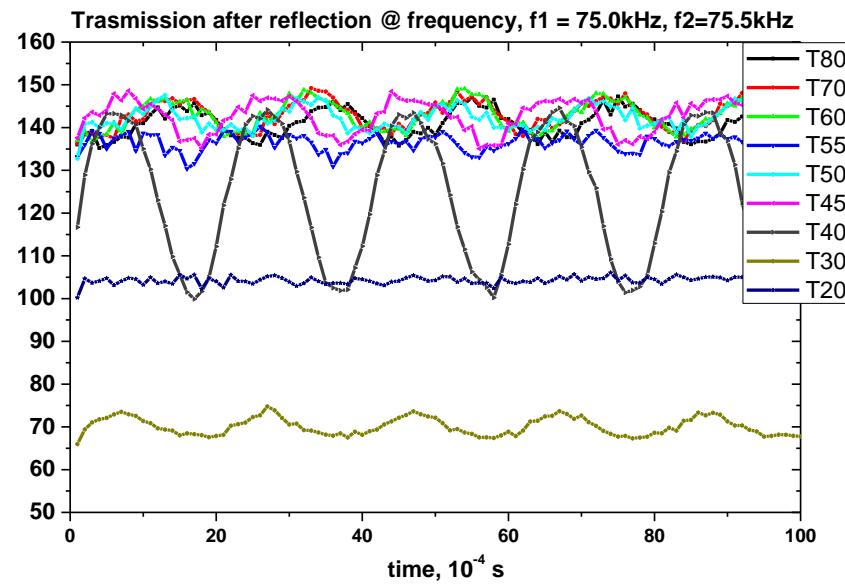
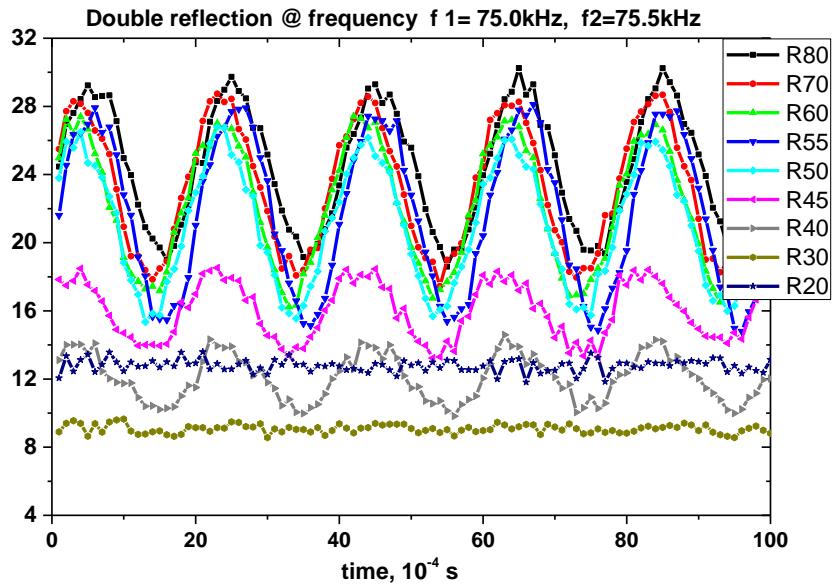
# Hysteresis loop from periodic [FeSi]<sub>x</sub>40 multilayer



# Heterodyne effect measured @ RESEDA (FRM2-Muenchen, 2014)



# Heterodyne @ fH=500 Hz for frequencies f=75 kHz & 0.4 MHz



# Phase variation

$$\bar{\phi} = [(L_2 / L_1) - (\omega_1 / \omega_H)](\omega_H L_1 / \bar{v}_n)$$

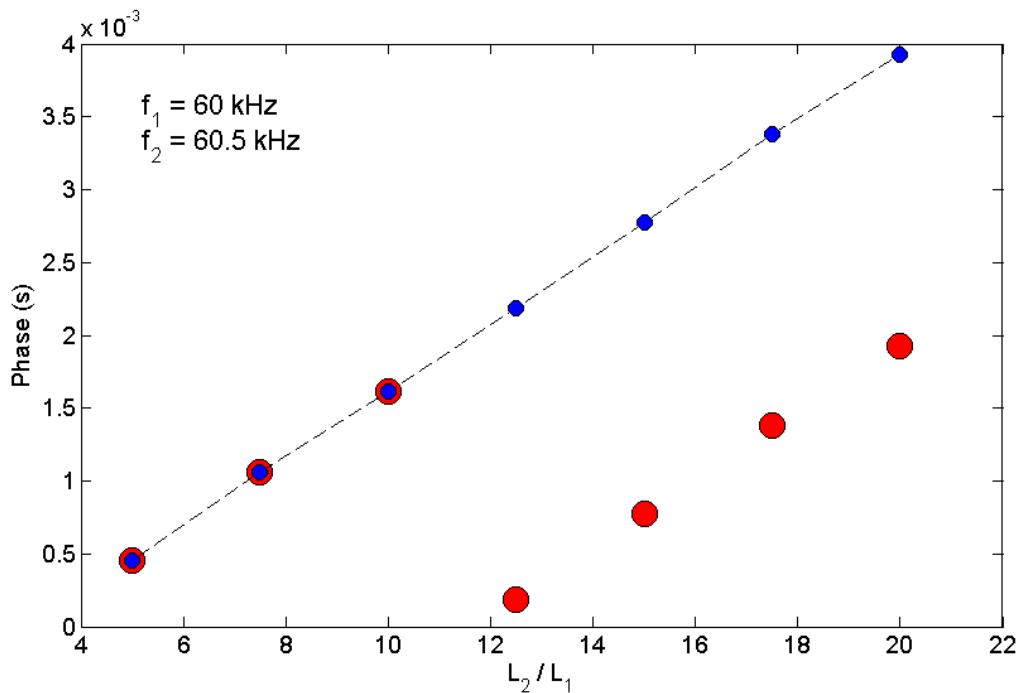
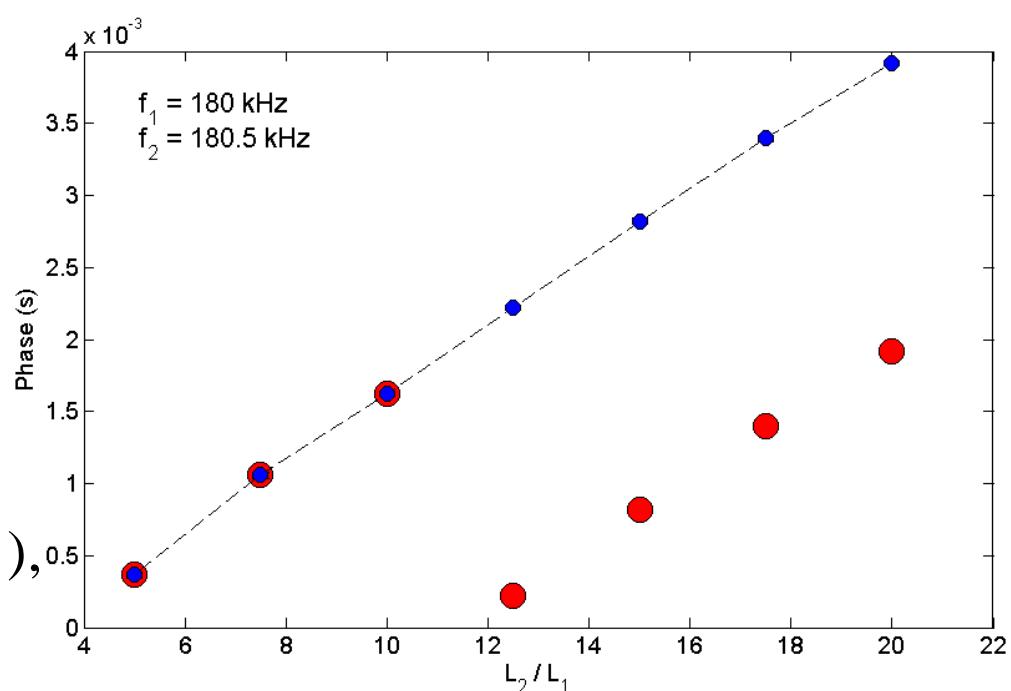
$$L_1 = 19 \text{ cm}, \lambda = 5.5 \text{ \AA}$$

$$f_H = 0.5 \text{ kHz}, f_1 = 60 \text{ kHz},$$

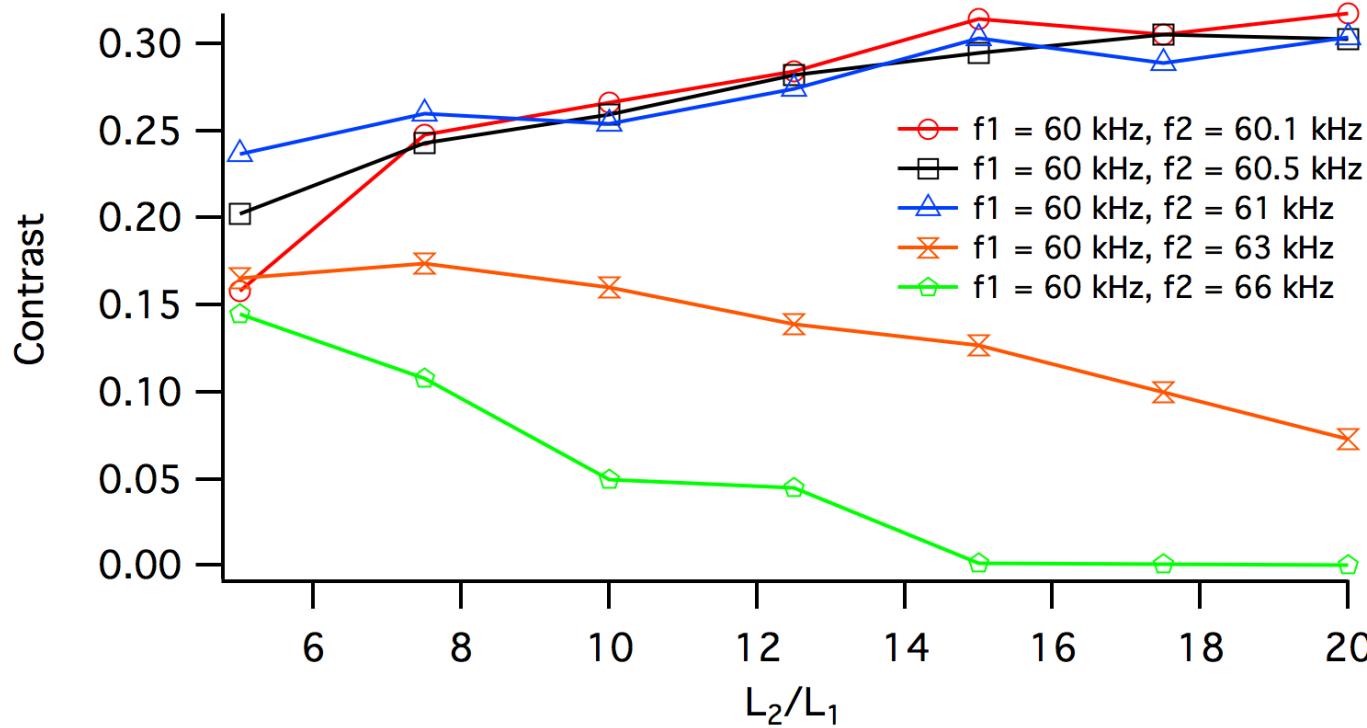
$$(\omega_H / \omega_1) = 120$$

$$\bar{\phi} = 0.13 \cdot (L_2 / L_1) - 5 \cdot \pi$$

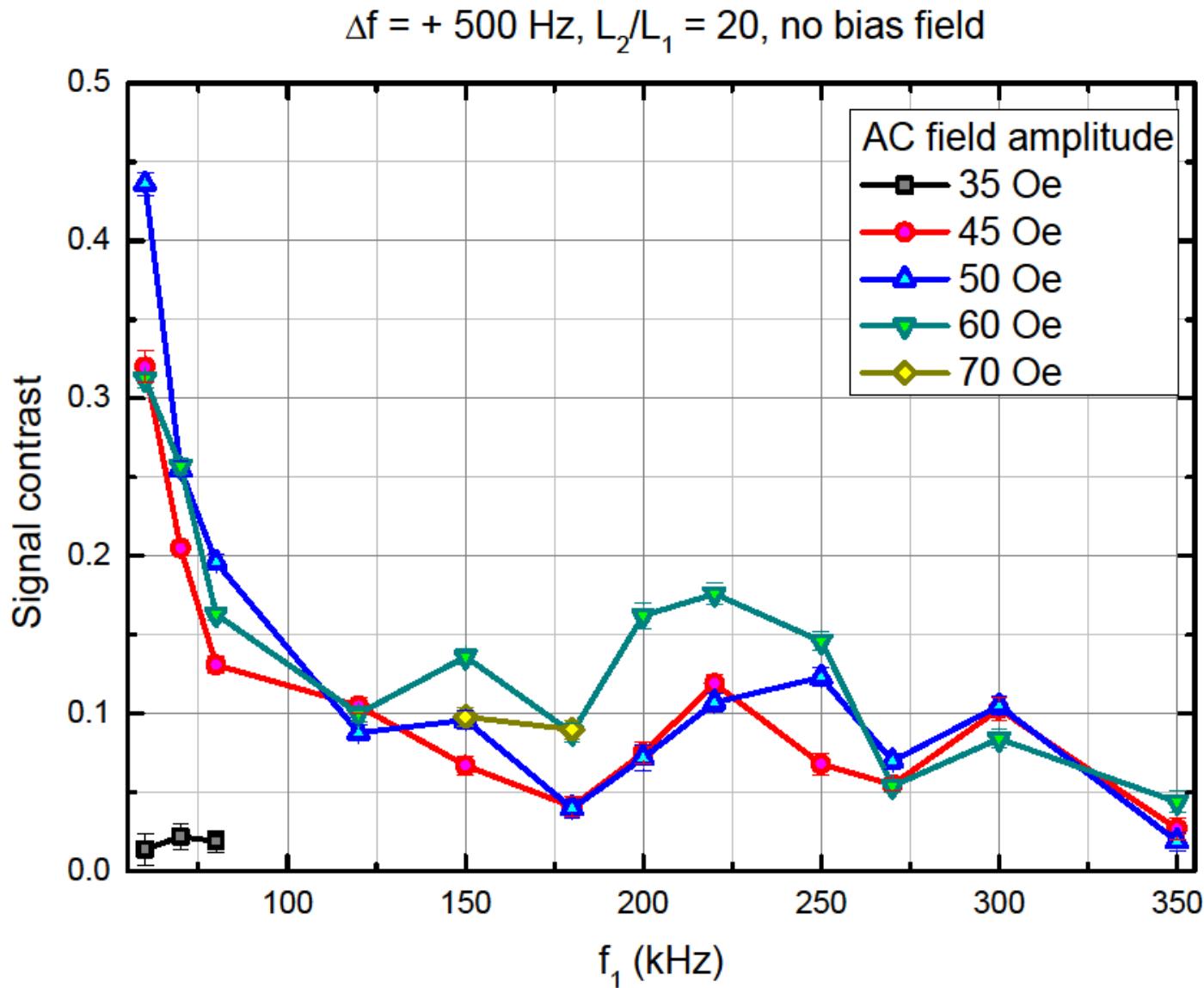
$$(\Delta\lambda / \lambda) = 0.1$$



# Heterodyne modulation contrast



# Frequency scans at different ac amplitudes



# *Conclusions*

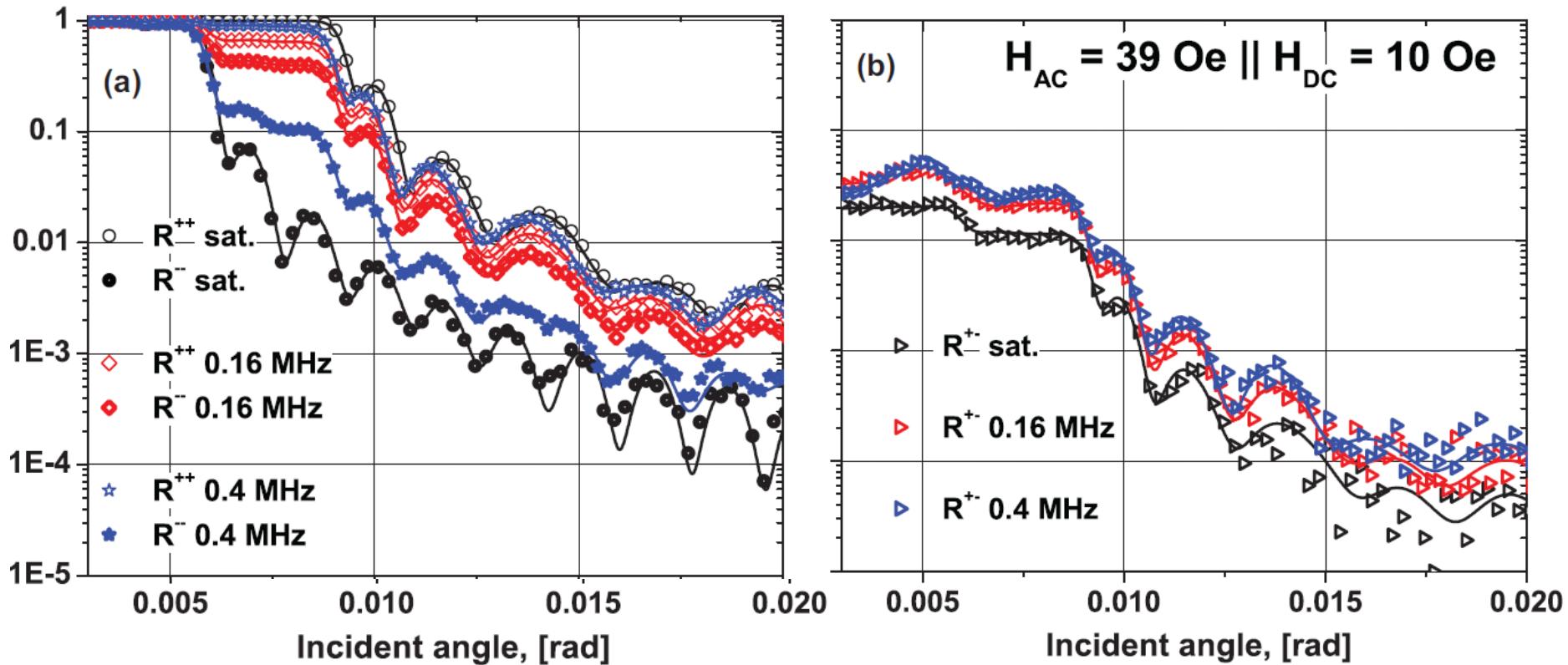
Heterodyne effect is experimentally proven to work  
with broad wavelength spread

Prototype of the spectrometer fro TRAC PNR is built

Perspectives for development of e.g. spin-echo spectrometer  
for inelastic PNR are suggested

## Frequency dependence of magnetization reversal in thin Fe(100) films

K. Zhernenkov,<sup>1,\*</sup> D. Gorkov,<sup>1</sup> B. P. Toperverg,<sup>1,2</sup> and H. Zabel<sup>1</sup>



Integrated over time PNR from 100 nm Fe film  
in AC field parallel to DC field and one of easy axes

# Frequency dependence of fitting parameters

$$\langle R^{++} \rangle_t = \frac{1}{4} |R_+(1 + \bar{c}_\gamma) + R_-(1 - \bar{c}_\gamma)|^2$$

$$\langle R^{--} \rangle = \frac{1}{4} |R_+(1 - \bar{c}_\gamma) + R_-(1 + \bar{c}_\gamma)|^2$$

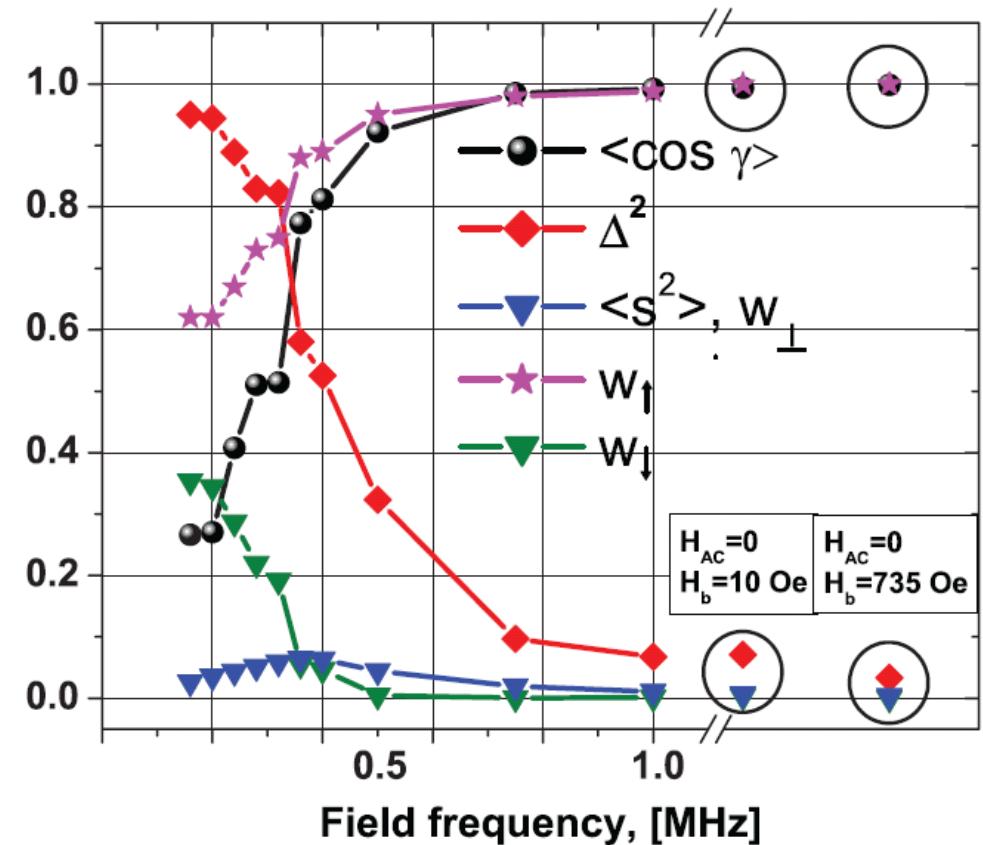
$$\langle R^{+-} \rangle = \langle R^{-+} \rangle = \frac{1}{4} |R_+ - R_-|^2 \overline{s_\gamma^2}$$

$$\bar{c}_\gamma = \frac{1}{T} \int_0^T dt \cos \gamma(t) = w_\uparrow - w_\downarrow$$

$$\overline{s_\gamma^2} = \frac{1}{T} \int_0^T dt \sin^2 \gamma(t) = w_\perp$$

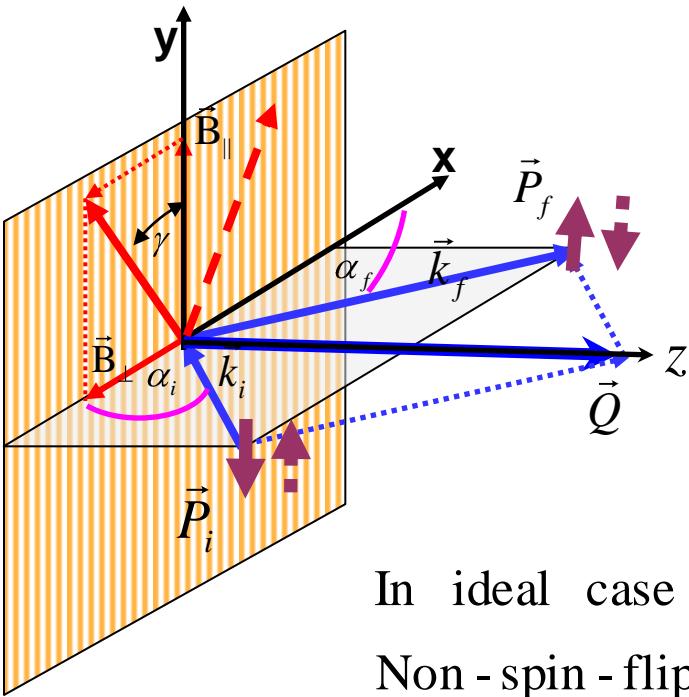
$$w_\uparrow - w_\downarrow + w_\perp = 1$$

$\Delta = \langle \cos^2 \gamma \rangle - \langle \cos \gamma \rangle^2$  is dispersion



@ 400 kHz crossover from  
180°+ 90° DW to 180°DW

# General Equation for PNR with 1D polarization analysis



If  $\vec{P}_{i,f} = \{0, \pm P_{i,f}, 0\}$ , then  $(\vec{P}_{i,f} \cdot \vec{b}) = \pm P_{i,f} \cos \gamma$ ,

$$R = \frac{1}{4} [ |R_+|^2 + |R_-|^2 ] [ P_i \cdot P_f \cdot \langle \cos^2 \gamma \rangle ]$$

$$+ \frac{1}{4} [ |R_+|^2 - |R_-|^2 ] [ P_i \cdot P_f \cdot \langle \cos \gamma \rangle ]$$

$$+ \frac{1}{2} \operatorname{Re} (\mathcal{R}_+^* R_-) [ P_i \cdot P_f \cdot \langle \sin^2 \gamma \rangle ]$$

In ideal case  $P_{i,f} = \pm 1$

Non - spin - flip reflectivities :

$$R^{\pm\pm} = \frac{1}{4} < (1 \pm \cos \gamma) \cdot R^+ + (1 \mp \cos \gamma) \cdot R^- >^2$$

Spin - flip - reflectivities :

$$R^{\pm\mp} = \frac{1}{4} < |R^+ - R^-|^2 \cdot \sin^2 \gamma >$$

where averaging runs over reflecting surface and time

# Time averaged PNR for crossed DC and AC fields (with polarization parallel DC field)

